# Topic 10

Multi-pitch Analysis

## What is pitch?

 "Common elements of music are **pitch**, rhythm, dynamics, and the sonic qualities of timbre and texture."

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---- Wikipedia
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- An auditory perceptual attribute in terms of which sounds may be ordered from low to high.
- For (quasi) harmonic sound e.g. a flute note, it is well defined by the Fundamental Frequency (F0).

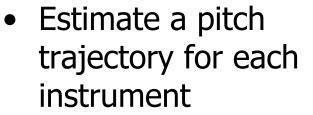


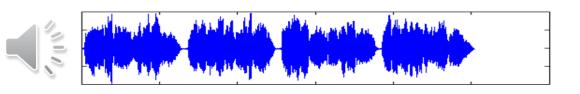
• A mixture of (quasi) harmonic sounds has multiple pitches (F0s).

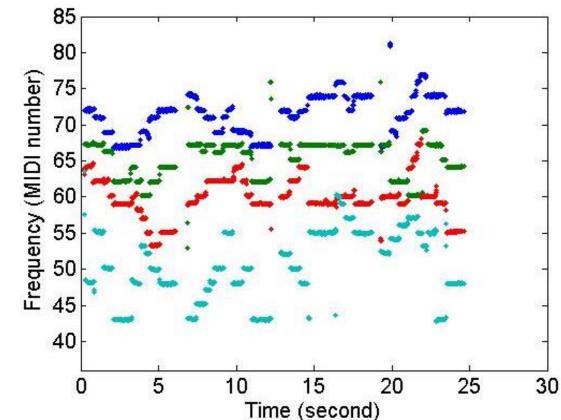
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#### **Multi-pitch Analysis of Polyphonic Music**

 Given polyphonic music played by several harmonic instruments







# Why is it important?

- A fundamental problem in computer audition for harmonic sounds
- Many potential applications
  - Automatic music transcription
  - Harmonic source separation
  - Melody-based music search
  - Chord recognition
  - Music education

— .....



### How difficult is it?

<ul> <li>Let's do a test!</li> </ul>	Chord 1	Chord 2
<ul> <li>Q1: How many pitches are there?</li> </ul>	2	3
<ul> <li>Q2: What are their pitches?</li> </ul>	C4/G4	C4/F4/A4
<ul> <li>Q3: Can you find a pitch in Chord 1 and a pitch in Chord 2 that are played</li> </ul>	Clarinet G4 Horn C4	Clarinet A4 Viola F4 Horn C4
by the same instrument?		

## We humans are amazing!

- "In Rome, he (14 years old) heard Gregorio
   Allegri's *Miserere* once in performance in the Sistine
   Chapel. He wrote it out
   entirely from memory, only returning to correct
   minor errors..."
  - -- Gutman, Robert (2000). *Mozart: A Cultural Biography*

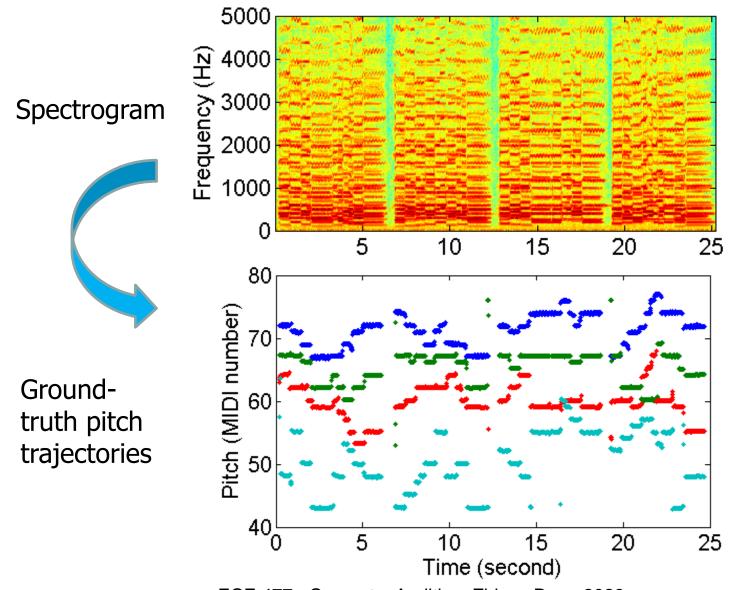


Wolfgang Amadeus Mozart

•Can we make computers compete with Mozart??

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#### **Our Task**



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### Subtasks in Multi-pitch Analysis

Three levels according to MIREX:

- Level 1: Multi-pitch Estimation (MPE)
  - Estimate pitches and polyphony in each time frame
- Level 2: Note Tracking
  - Track pitches within a note
- Level 3: Streaming (timbre tracking)
  - Estimate a pitch trajectory for each source (instrument) across multiple notes

#### **Recent Methods**

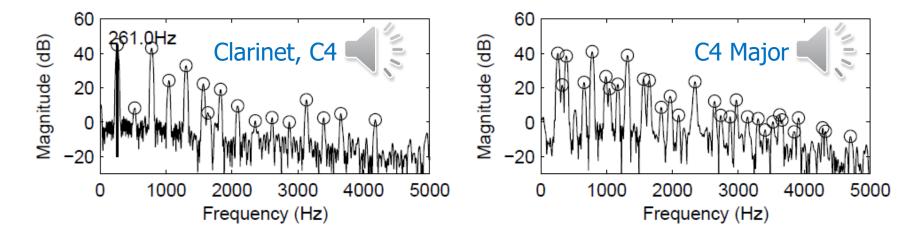
- Level 1: Multi-pitch Estimation
  - Klapuri'03, Goto'04, Davy'06, Klapuri'06, Yeh'05, Emiya'07, Pertusa'08, Duan'10, etc.
- Level 2: Note Tracking
  - Ryynanen'05, Kameoka'07, Poliner'07, Lagrange'07, Chang'08, Benetos'11, Cogliati'16, Ewert'17, Hawthorne'18, etc.
- Level 3: Streaming (timbre tracking)
  - Vincent'06, Bay'12, Duan'14

# Level 1: Multi-pitch Estimation

Estimate pitches in each single frame

## Multi-pitch Estimation (MPE)

• Why difficult?



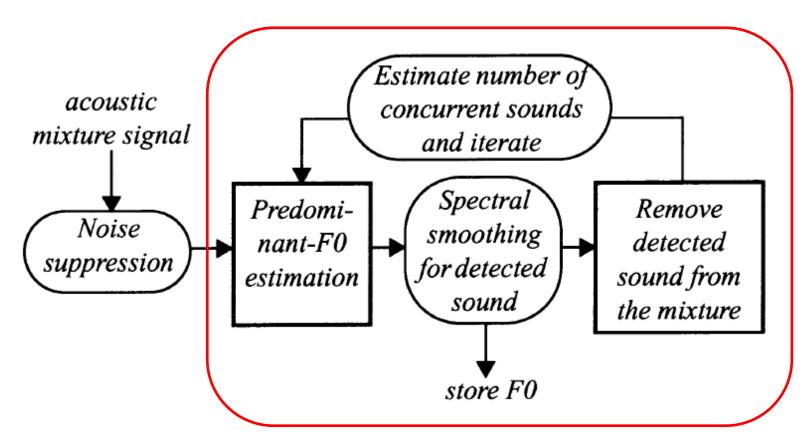
- Overlapping harmonics
  - C4 (46.7%), E4 (33.3%), G4 (60%)
- How to associate the 28 significant peaks to sources?
- Instantaneous polyphony estimation
- Large hypothesis space

### **Two Methods at Level 1**

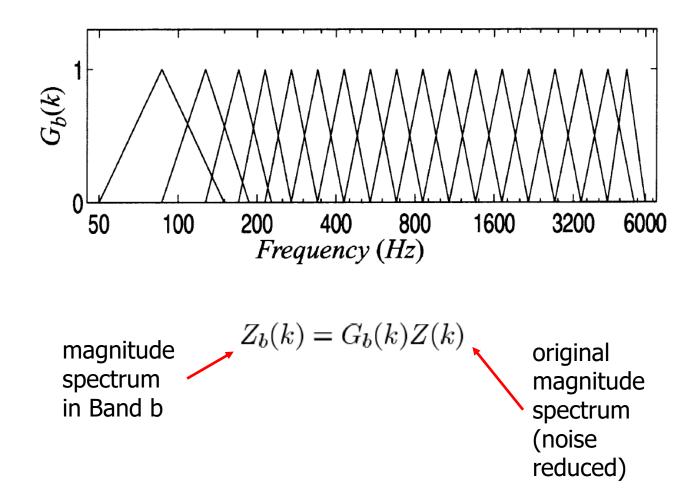
- Iterative spectral subtraction – [Klapuri, 2003]
- Probabilistic modeling of peaks and non-peak regions
  - [Duan et al., 2010]

#### **Iterative Spectral Subtraction**

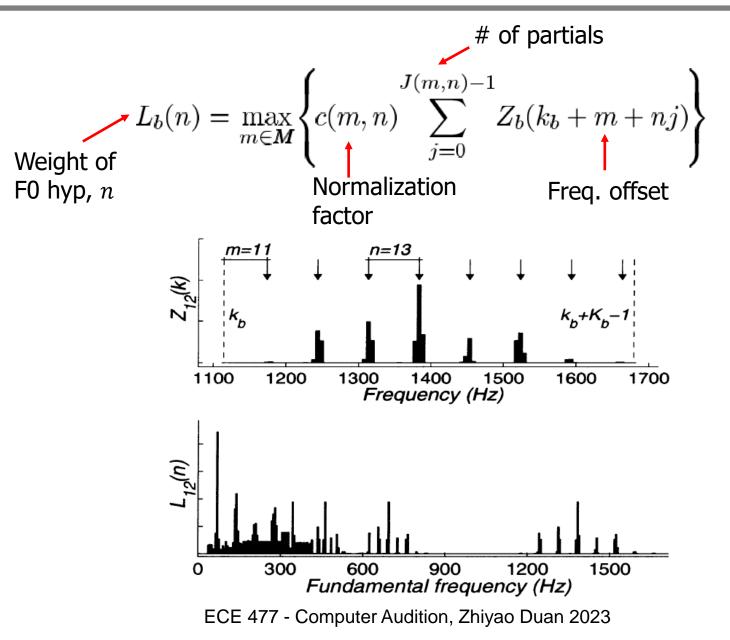
[Klapuri, 2003]



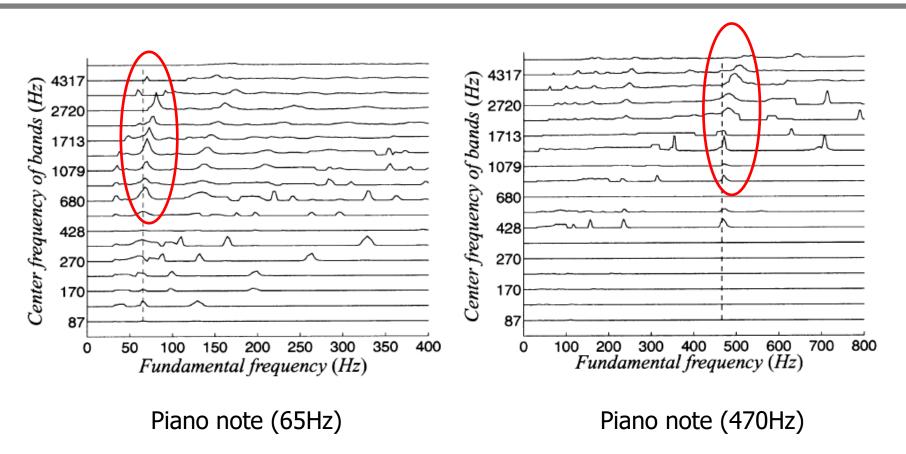
#### **Bandwise F0 Estimation**



#### **Bandwise F0 Estimation**



#### **Integrate Weights Across Subbands**



• Inharmonicity of higher harmonics should be considered

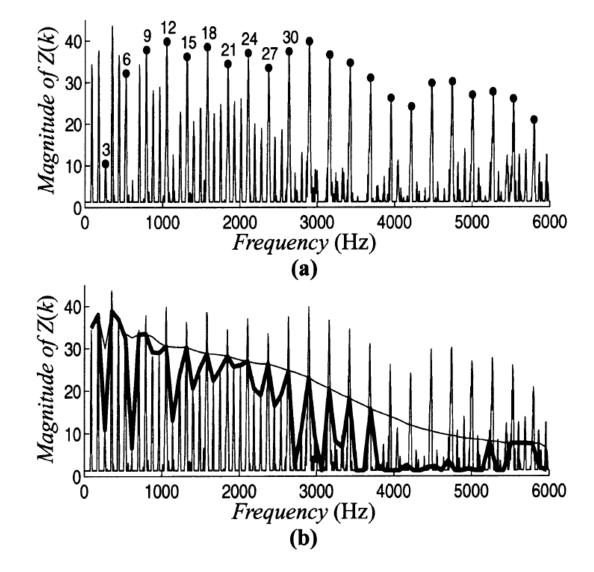
$$f_h = hF\sqrt{1 + (h^2 - 1)\beta}$$

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### **Spectral Subtraction**

- Given the estimated predominant F0, we can find out all its harmonics and subtract their energy from the mixture spectrum.
- How much energy should we subtract?
  - All?
  - Some harmonics are overlapped by those of other F0s, hence their energy is larger.

#### **Spectral Smoothness**



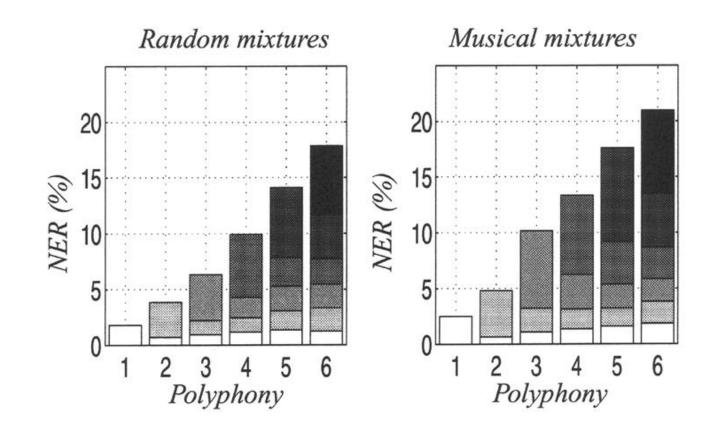
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## **Polyphony Estimation**

• I.e., when to stop the iterations?

• Stop if the energy of the harmonics of the estimated predominant F0 is smaller than a threshold.

### **Error Rate**



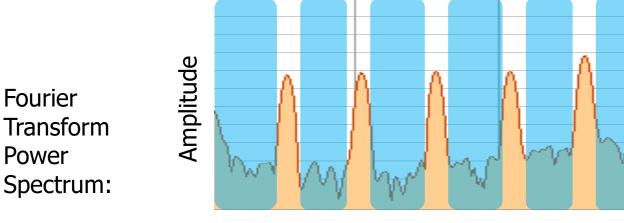
• More errors in later iterations

### Discussions

- Advantages
  - Simple idea
  - Fast algorithm
  - Handles inharmonicity
- Disadvantages
  - Spectra in later iterations are severely corrupted
  - Spectral smoothness is not enough to determine the amount of energy to subtract
- Why bandwise estimation?

## **Probabilistic Modeling of Peaks**

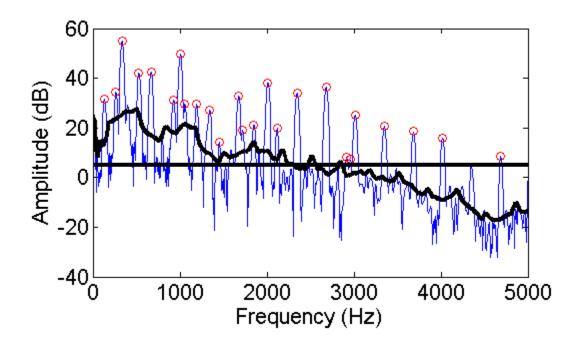
- A maximum likelihood estimation method  $\widehat{\boldsymbol{\theta}} = \arg \max_{\boldsymbol{\theta} \in \boldsymbol{\Theta}} p(\boldsymbol{\theta}|\boldsymbol{\theta}) \quad \text{[Duan et al., 2010]}$ Best pitch estimate (a set of pitches) Observed power spectrum Pitch hypothesis, (a set of pitches)
- Spectrum: peaks & the non-peak region



**Frequency** ECE 477 - Computer Audition, Zhiyao Duan 2023

### **Peaks / Non-peak Region**

• Peaks: ideally correspond to harmonics



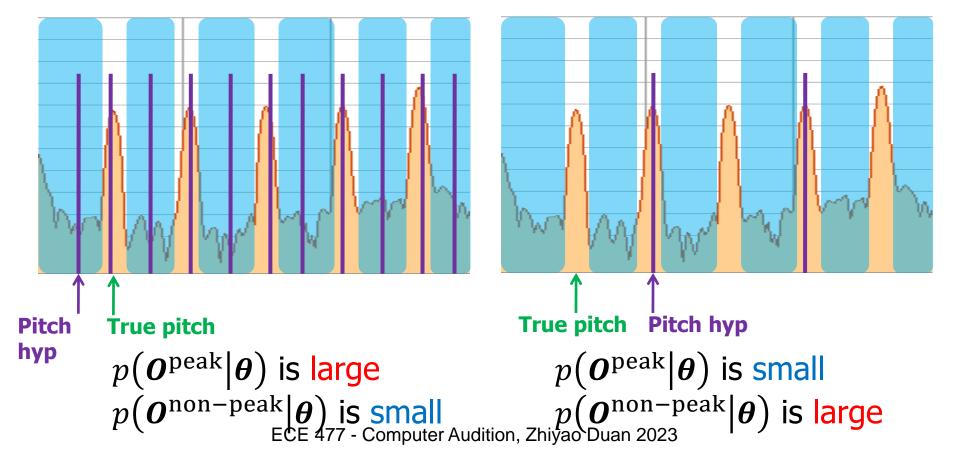
• Non-peak region: frequencies further than a threshold from any peak

#### **Likelihood as Dual Parts**

$$p(\boldsymbol{\theta}|\boldsymbol{\theta}) = p(\boldsymbol{\theta}^{\text{peak}}|\boldsymbol{\theta}) \cdot p(\boldsymbol{\theta}^{\text{non-peak}}|\boldsymbol{\theta})$$

Probability of observing these peaks:  $(f_k, a_k), k = 1, ..., K$ .

Probability of not having any harmonics in the non-peak region

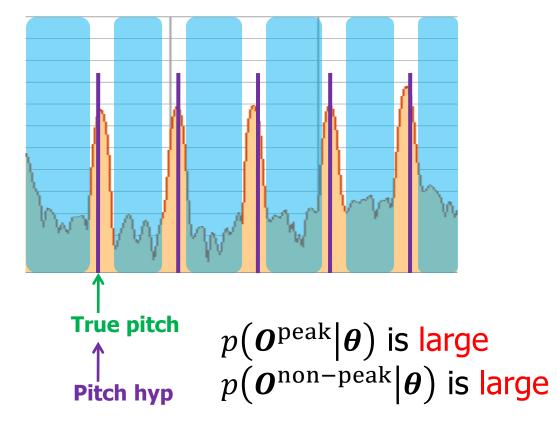


#### **Likelihood as Dual Parts**

$$p(\boldsymbol{\theta}|\boldsymbol{\theta}) = p(\boldsymbol{\theta}^{\text{peak}}|\boldsymbol{\theta}) \cdot p(\boldsymbol{\theta}^{\text{non-peak}}|\boldsymbol{\theta})$$

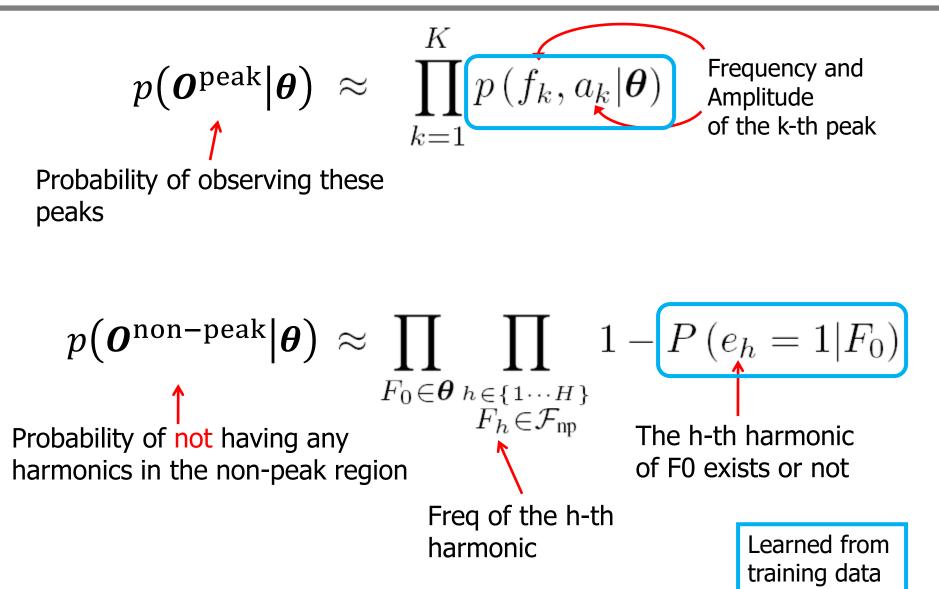
Probability of observing these peaks:  $(f_k, a_k), k = 1, ..., K$ .

Probability of not having any harmonics in the non-peak region



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#### **Likelihood Models**



## **Model Training**

- For polyphonic music
  - 3000 random chords of polyphony 1 to 6
  - Mixed using note samples from 16 instruments with pitch ranges from C2 (65 Hz) to B6 (1976 Hz)

- For multi-talker speech
  - 500 speech excerpts with 1-3 simultaneous talkers
  - Mixed from single-talker speech

• Obtained ground-truth pitches before mixing

### **Greedy Search Algorithm**

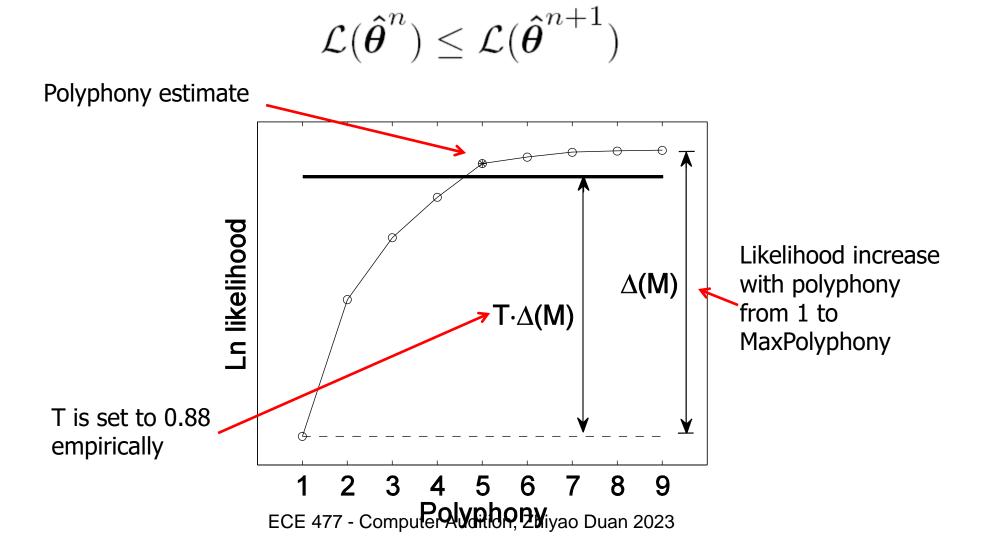
$$\widehat{\boldsymbol{\theta}} = \arg \max_{\boldsymbol{\theta} \in \boldsymbol{\Theta}} p(\boldsymbol{\theta} | \boldsymbol{\theta})$$

- Parameter space is too big for exhaustive search
- Greedy search algorithm
  - Initialize  $\theta = \emptyset$
  - For i = 1 to *MaxPolyphony* 
    - Add a pitch to  $\theta$ , s.t. likelihood increases
  - End
  - Estimate polyphony N
  - Return the first N pitches of  $\boldsymbol{\theta}$



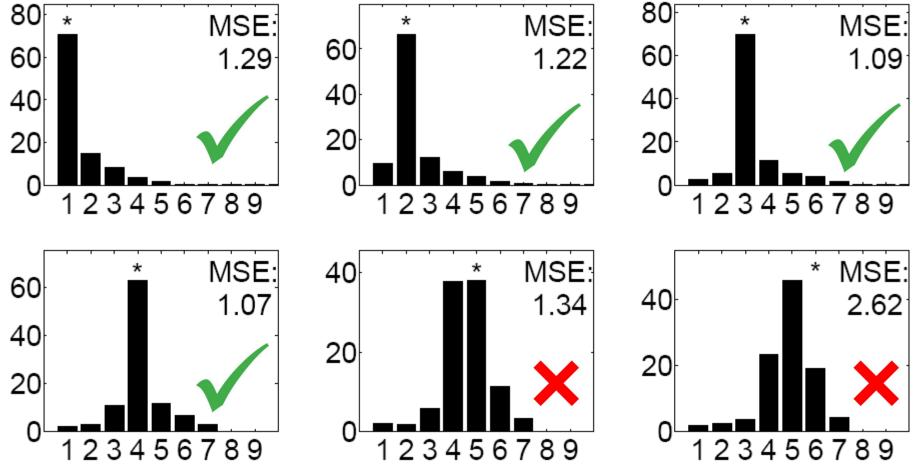
# **Polyphony Estimation**

• Likelihood increases with estimated polyphony



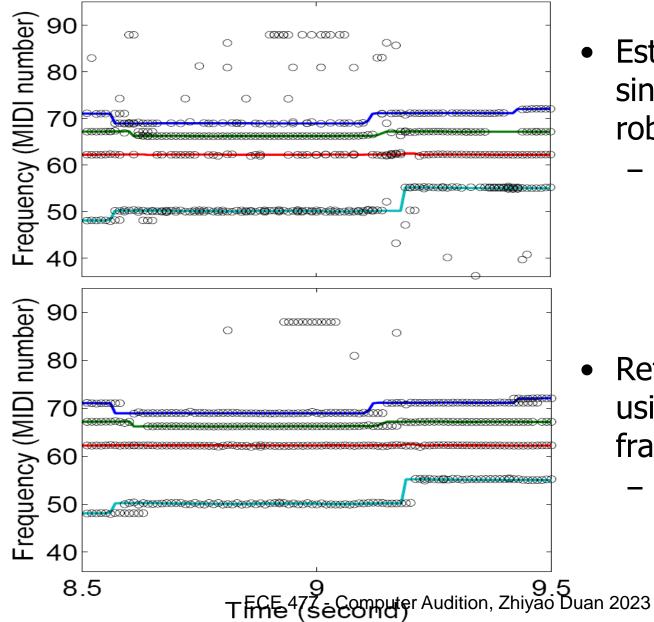
### **Experiments – Polyphony Estimation**

• 6000 musical chords mixed using notes unseen in training data (1000 for each polyphony)



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## **Post Processing**



- Estimation in each single frame is not robust
  - Insertion, deletion and substitution errors

- Refine estimates using neighboring frames
  - Only keep consistent estimates

#### **Discussions**

- Advantages
  - Model parameters can be learned from training data

- Disadvantages
  - Assumes conditional independence of peak amplitudes, given F0s
  - Doesn't consider the relation between peak amplitudes, e.g., spectral smoothness

## Level 2: Note Tracking

Estimate a pitch trajectory for each note

### **Two Methods at Level 2**

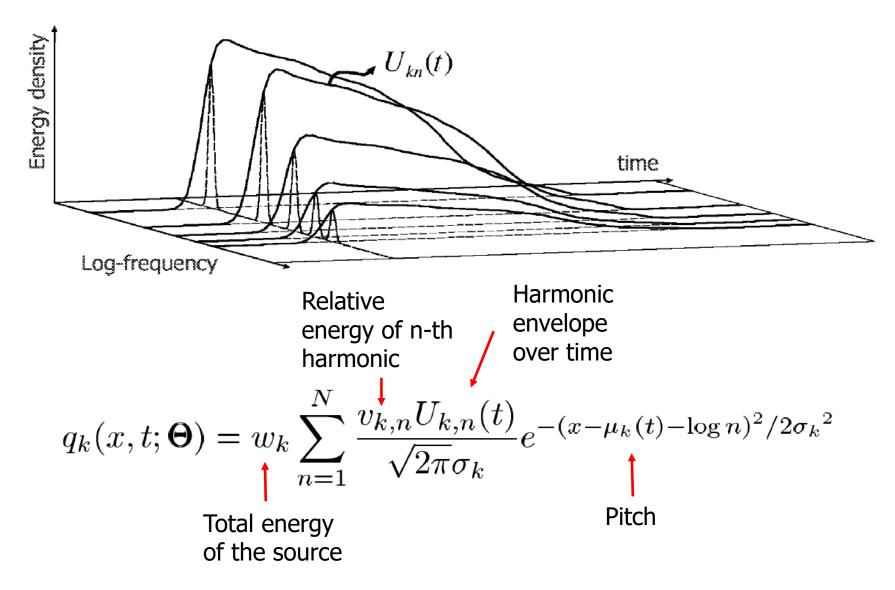
- Probabilistic modeling of the spectral-temporal content a note of a source
  - [Kameoka, et al., 2007]

- Classification-based piano note transcription
  - [Poliner & Ellis, 2007]
  - [Hawthorne, et al., 2018]

[Kameoka et al, 2007]

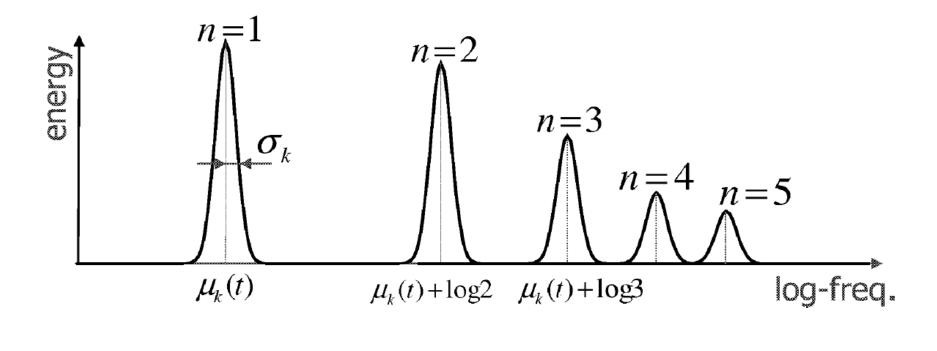
- Jointly estimates pitch, intensity, onset, duration of notes.
- Detailed parametric model for the spectral content of a note of a source
- Approximating the spectrogram with superimposed HTC source models

#### **HTC Source Model**



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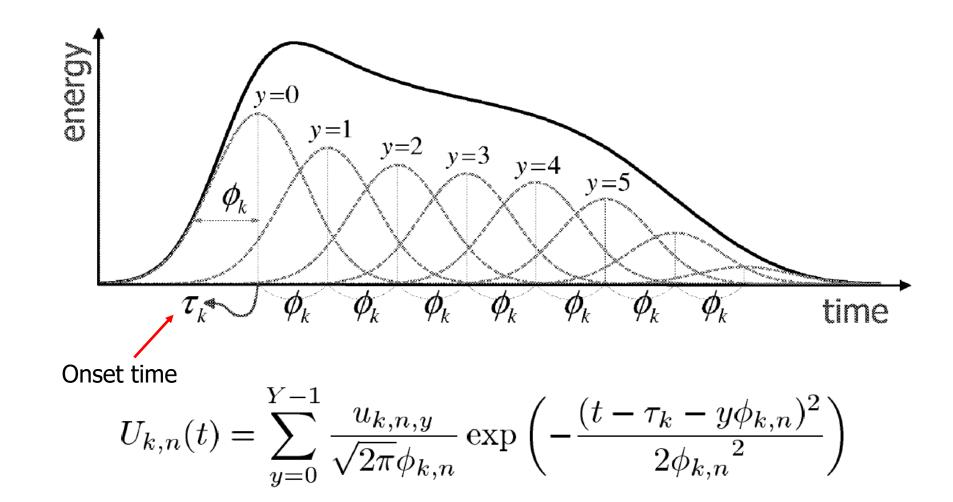
#### The Model in A Single Frame



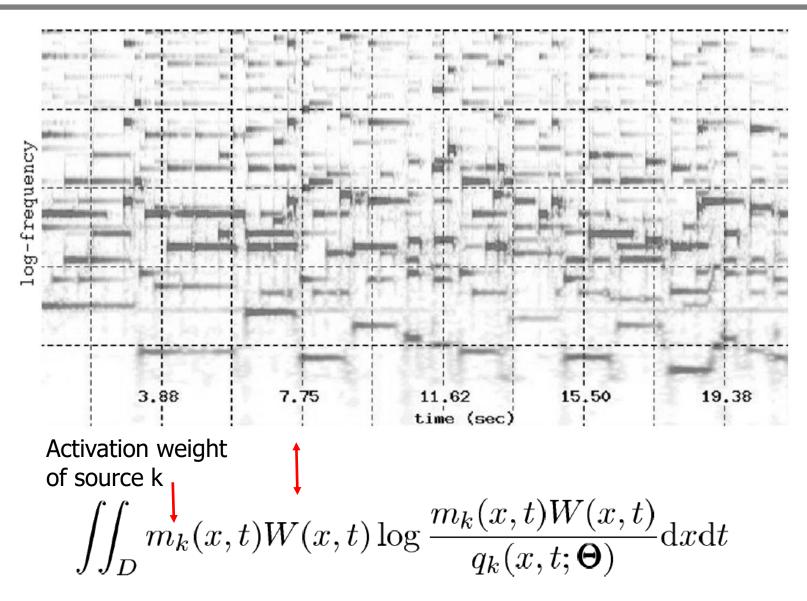
$$q_k(x,t;\Theta) = w_k \sum_{n=1}^{N} \frac{v_{k,n} U_{k,n}(t)}{\sqrt{2\pi}\sigma_k} e^{-(x-\mu_k(t)-\log n)^2/2\sigma_k^2}$$

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#### **Harmonic Envelope**



## **Reconstruction using HTC models**



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# **The Unknowns**

- Model parameters
  - Pitch, onset time, harmonic width, harmonic envelope over time, duration, etc.
- Latent variable
  - Activation weights of sources
- EM algorithm

#### Discussions

- Advantages
  - Very detailed model
  - Jointly estimates pitch, onset, duration, etc.

- Disadvantages
  - Model is very complicated

#### **Classification-based Piano Note Transcription**

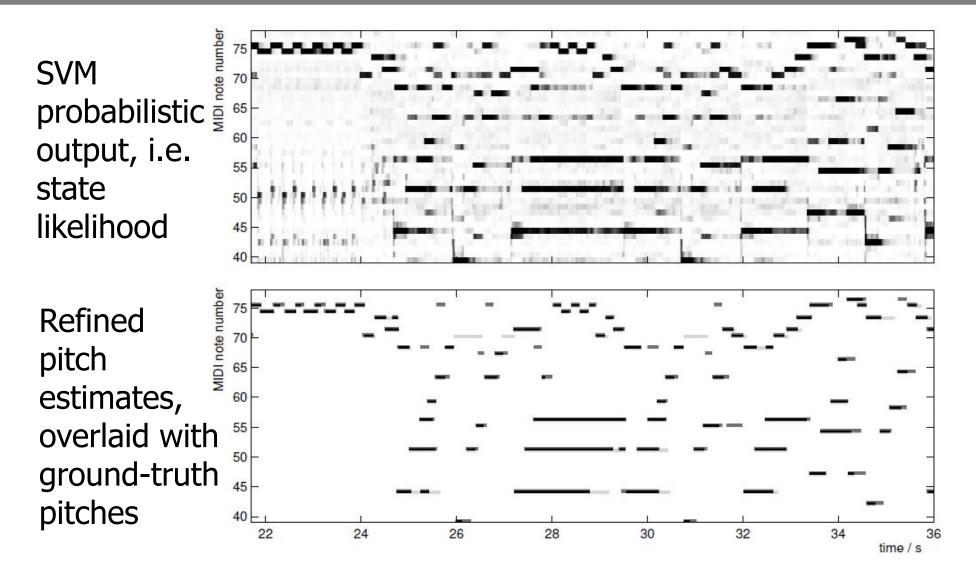
[Poliner & Ellis, 2007]

- Train 88 (one-versus-all) SVM classifiers, one for each key of piano, from training audio frames
- Multi-label classification on each frame of the test audio
- Data: MIDI synthesized audio + Yamaha Disklavier playback grand piano
- Feature: a part of the magnitude spectrum

# **HMM Post Processing**

- 88 HMMs, one for each key
- 2 states: the pitch (key) is on/off
- Transition probability: learned from training data
- Observation probability (state likelihood): the probabilistic output of SVMs
- Viterbi algorithm to refine pitch estimates

#### **HMM Post Processing Result**



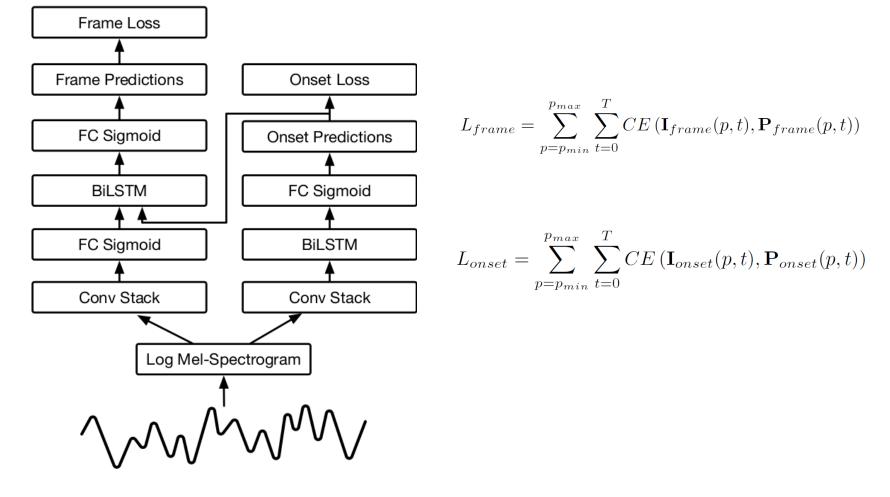
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# Discussions

- Advantages
  - The first classification-based transcription method
  - Simple idea
  - Easy to implement
- Disadvantages
  - The classification and post-processing of piano keys are performed totally independently
  - Induces more octave errors

#### **Classification-based Piano Note Transcription**

[Harthorne et al., 2018]



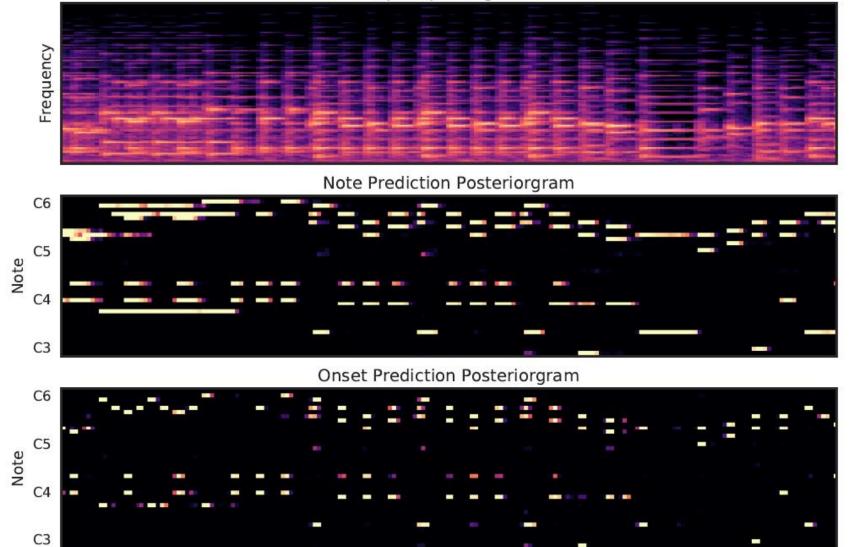
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# **Model Training**

- Training data
  - MAPS dataset: MIDI synthesized audio + Yamaha Disklavier playback grand piano
- Trained for 5 hours on 3 P100 GPUs

#### **Example Output**

Input Spectrogram



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#### **Results**

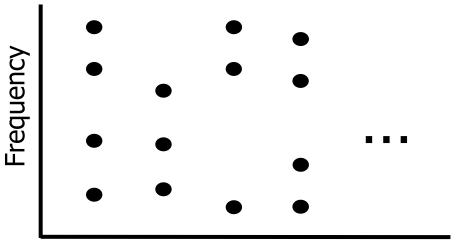
	Frame			Note			Note w/ offset			Note w/ offset & velocity		
	Р	R	F1	Р	R	F1	Р	R	F1	Р	R	F1
Sigtia et al., 2016 [18]	71.99	73.32	72.22	44.97	49.55	46.58	17.64	19.71	18.38	_		_
Kelz et al., 2016 [13]	81.18	65.07	71.60	44.27	61.29	50.94	20.13	27.80	23.14			—
Melodyne (decay mode)	71.85	50.39	58.57	62.08	48.53	54.02	21.09	16.56	18.40	10.43	8.15	9.08
Onsets and Frames	88.53	70.89	78.30	84.24	80.67	82.29	51.32	49.31	50.22	35.52	30.80	35.39

# Level 3: Multi-pitch Streaming

# Estimate a pitch trajectory for each harmonic source

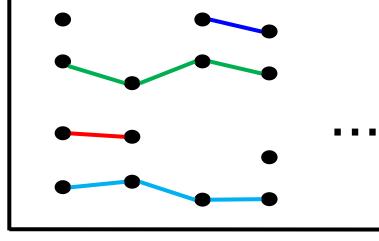
# A 2-stage System

- Stage 1: Estimate pitches in each single time frame
  - [Duan et al., 2010]

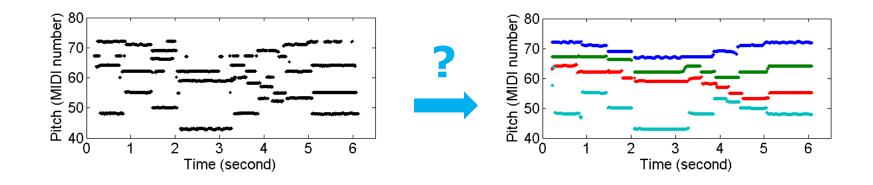




- Stage 2: Connect pitch estimates across frames into pitch trajectories
  - [Duan et al., 2014]



#### **How to Stream Pitches?**



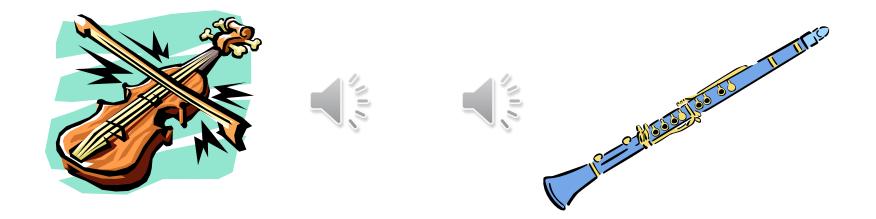
- Label pitches by pitch order in each frame, i.e. highest, second highest, third highest, ...?
- Connect pitches by continuity?
  - Only achieves note tracking

# **Clustering Pitches by "Timbre"!**

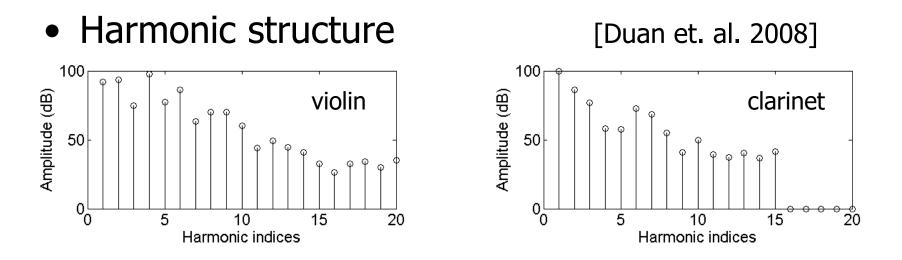
• Human use timbre to discriminate and track sound sources

"Timbre is that attribute of sensation in terms of which a listener can judge that two sounds having the same **loudness** and **pitch** are dissimilar."

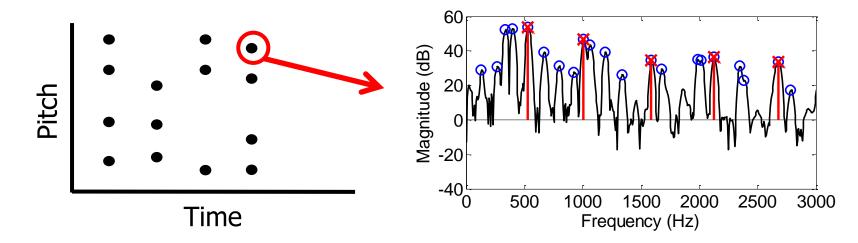
---- American Standards Association



# **How to Represent Timbre?**

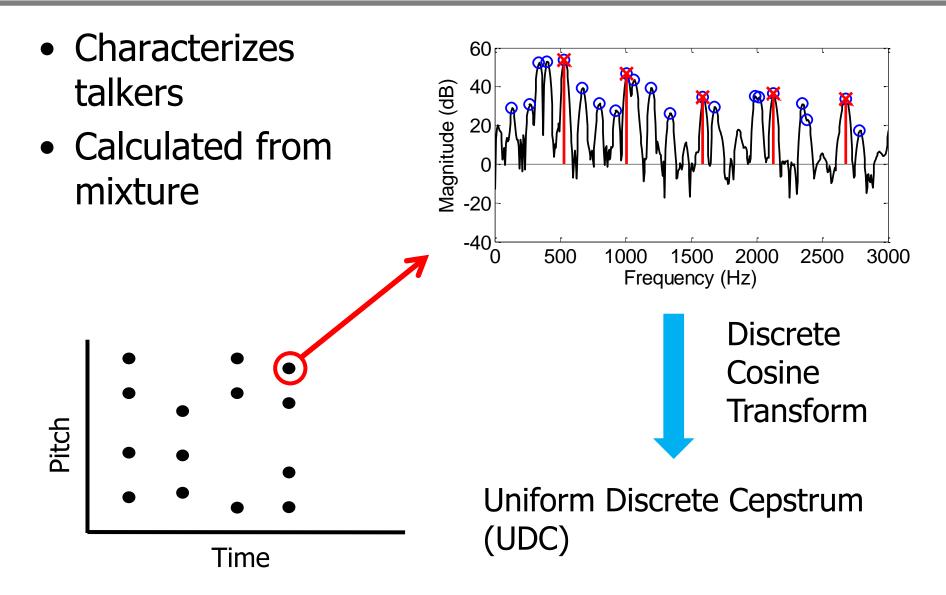


• Calculate for each pitch from the mixture



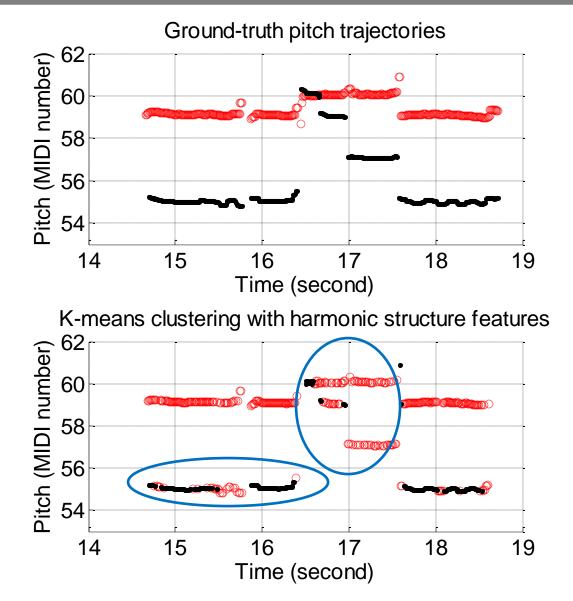
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## **Timbre Feature for Talkers**



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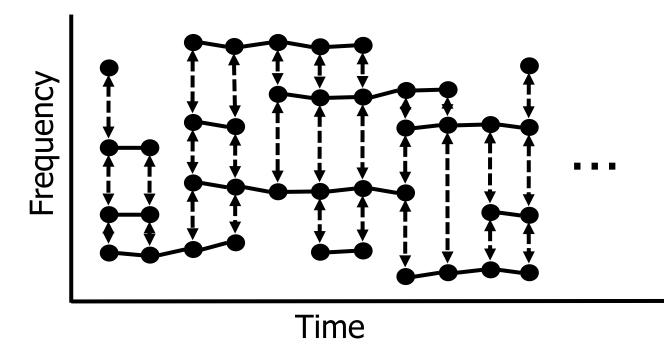
# Clustering by timbre is not enough



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# **Use Pitch Locality Constraints**

- Cannot-link: between simultaneous pitches (only for monophonic instruments)
- Must-link: between pitch estimates close in both time and frequency



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# **Constrained Clustering**

- Objective: minimize timbre inconsistency
- Constraints: pitch locality
  - Inconsistent constraints: caused by incorrect pitch estimates, interweaving pitch trajectories, etc.
  - Heavily constrained: nearly every pitch estimate is involved in at least one constraint
- Algorithm: iteratively update the clustering s.t.
  - The objective monotonically decreases
  - The set of satisfied constraints monotonically expands

# **The Proposed Algorithm**

- *f*: objective function; *C*: all constraints;
- $\Pi_n$ : clustering in *n*-th iteration;
- $C_n$ : {constraints satisfied by  $\Pi_n$ };

• It converges to some local minimum  $< \Pi', C' >$ .

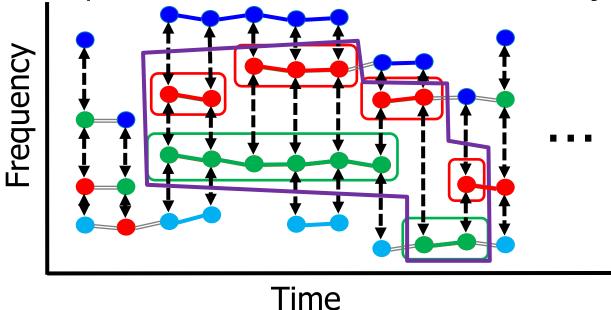
 $f(\Pi_0) > f(\Pi_1) > \dots > f(\Pi')$ 

 $\mathcal{C}_0 \subseteq \mathcal{C}_1 \subseteq \cdots \subseteq \mathcal{C}'$ 

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# Find A New Clustering to...

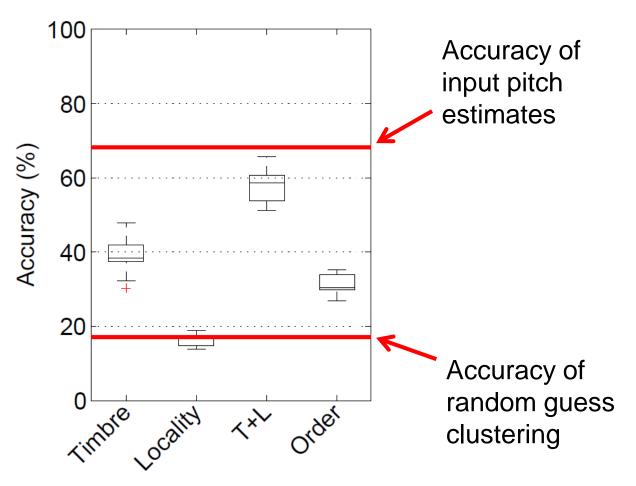
- 1. Decrease the objective function
- 2. Satisfy satisfied constraints
- Swap set: a connected graph between two clusters by already satisfied constraints
- One more must link is satisfied now
- Try all swap sets to find one that decreases objective



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#### **Timbre Objective & Locality Constraints**

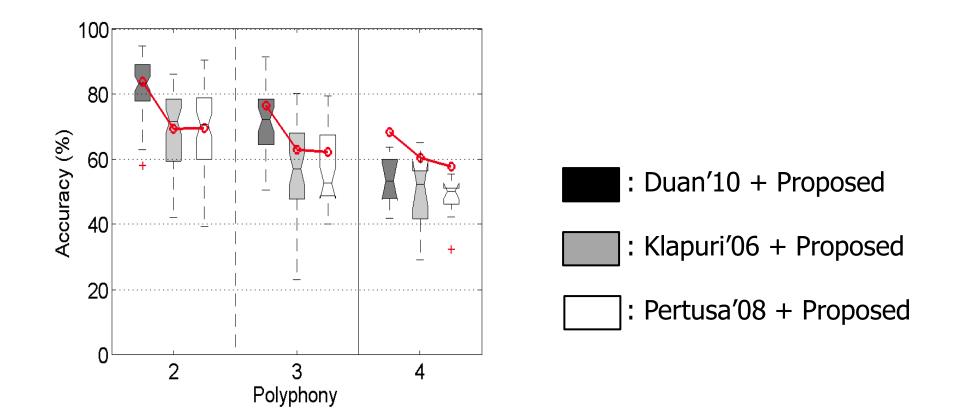
• Results on 10 quartets played by violin, clarinet, saxophone and bassoon



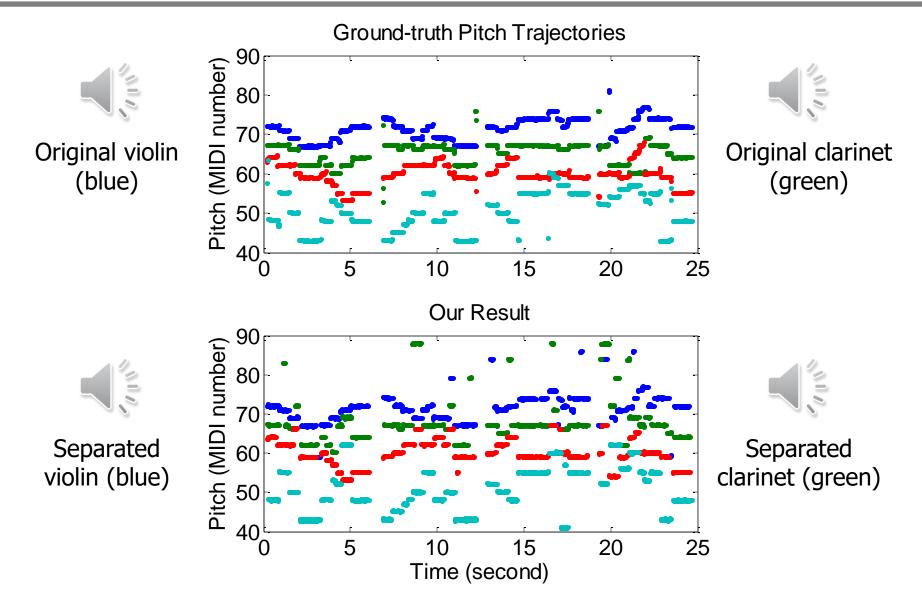
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## **Works with Different MPE Methods**

• Results on 60 duets, 40 trios, and 10 quartets



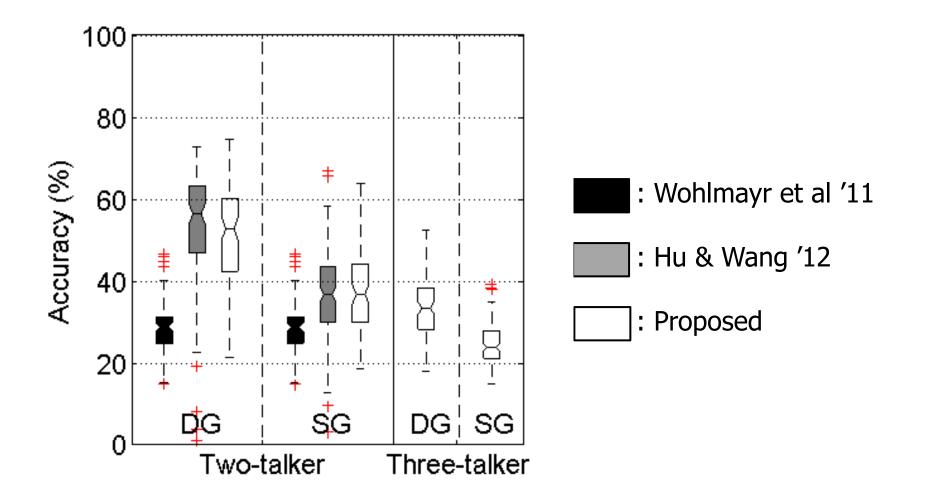
# **Example on Music**



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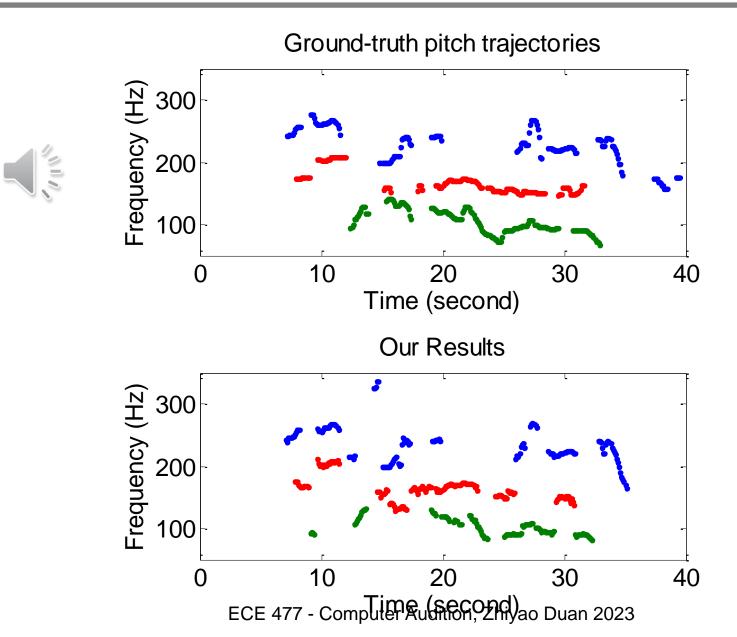
## **Comparisons on Speech**

• 400 2-talker and 3-talker speech excerpts



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## **Example on Speech**



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## Discussions

- Advantages:
  - Able to stream pitches across notes
  - Considers both timbre and pitch location info

- Disadvantages:
  - Algorithm is slow and complicated.
  - Constraints are binary.
  - Cannot deal with polyphonic instruments e.g. piano and guitar.